

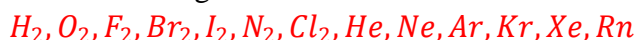
Monday/Tuesday - October 28 &amp; 29, 2019 - Properties of Gases &amp; Gas Stoichiometry: (Chapter 5 Pt 1)

**I. Big Idea –**

Let's think about the three physical states of substances: solid, liquid and gas. Today we're going to think about gas (*Solid and Liquid we'll do in 1C*). Chemical properties for gases vary significantly, but physical properties are simpler to talk about: Gases occupy the full **volume** of their containers. Gases also have a **pressure** and a **temperature**. By looking at these properties, we can understand the behavior of gases.

Pressure:  $1 \text{ atm} = 760 \text{ torr} = 760 \text{ mmHg}$ Temperature:  $T(\text{Kelvin}) = T(\text{Celsius}) + 273.15$ STP Conditions:  $273.15 \text{ K} (0 \text{ C}), 1 \text{ atm}$ SATP Conditions:  $298.15 \text{ K} (25 \text{ C}), 1 \text{ atm}$ 

11 elements are gases under standard conditions



As well as low molar mass compounds such as



Gases are **compressible**, and they fill up the space that is available. This implies that **the molecules are moving quickly in chaotic motion**.

**II. Pressure in Systems**

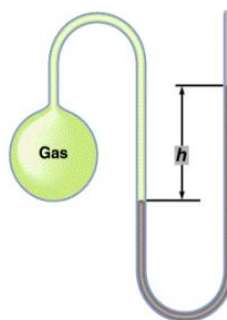
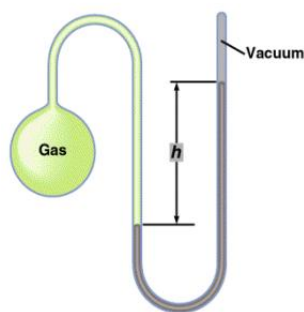
1. A glass column is filled with mercury and inverted in a pool of mercury. The mercury column stabilizes at a height of 735 mm above the pool of mercury. What is the pressure of the atmosphere?  $0.967 \text{ atm}$

**Barometers****Height = gravity + Pint + Pext**

2. Determine the pressure (atm) of the gas in the flask.

a.  $h = 0.15 \text{ m}$

b.  $h = 0.08 \text{ m}, P_{\text{atmosphere}} = 1 \text{ atm}$



$$h \text{ (in mm)} = |\Delta P \text{ (in torr)}|$$

$$h = |P_{\text{gas}} - P_{\text{vacuum}}|$$

$$h = 0.15 \text{ m} = 150 \text{ mm}$$

$$150 = |P_{\text{gas}} - 0|$$

$$P_{\text{gas}} = 150 \text{ torr}$$

$$150 \text{ torr} \frac{1 \text{ atm}}{760 \text{ torr}} = 0.197 \text{ atm}$$

$$h \text{ (in mm)} = |\Delta P \text{ (in torr)}|$$

$$h = |P_{\text{gas}} - P_{\text{atmosphere}}|$$

$$h = 0.08 \text{ m} = 80 \text{ mm}$$

$$80 = |P_{\text{gas}} - 760|$$

$$P_{\text{gas}} = 840 \text{ torr}$$

$$840 \text{ torr} \frac{1 \text{ atm}}{760 \text{ torr}} = 1.1 \text{ atm}$$

### III. The Ideal Gas Law: \_\_\_\_\_

1. What volume (in L) is occupied by 35.2 g of nitrogen at 35°C and 0.975 atm?

$$PV = nRT; m=35.2g, MW = 28.02 \text{ g/mol of } N_2$$

$$N = 35.2g N_2 (1 \text{ mol}/28.02 \text{ g } N_2) = 1.26 \text{ mol } N_2$$

$$T = 35C = 35 + 273.15 = 308K$$

$$V = nRT/P = (1.26 \text{ mol})(0.08206 \text{ Latm/molK})(308K)/(0.975 \text{ atm}) = 32.7L$$

What makes an ideal gas/ideal conditions?

- High temp
- Low pressure
- Small particle size
- Low interaction btw particles

2. A 36.4 L volume of methane gas is heated from 25°C to 88°C at constant pressure. What is the final volume of gas?

$$V_1/T_1 = V_2/T_2 \text{ and therefore } V_2 = V_1 * T_2/T_1 = (36.4L) * (361.15K)/(298.15K) = 44.1L$$

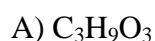
3. A sample of oxygen gas has a volume of 4.50 L at 27°C and 800.0 torr. How many oxygen molecules are in the sample?

# of molecules can be derived from moles

$$PV = nRT \quad n = \frac{PV}{RT} \quad n = \frac{(800 \text{ torr})(4.5L)}{(62.37 \text{ torrL/molK})(300K)} \quad n = 0.192 \text{ mol}$$

$$0.192 \text{ mol} \times 6.022 \times 10^{23} \text{ molecules/mol} = 1.16 \times 10^{23} \text{ molecules}$$

4. The empirical formula of a gas is CH<sub>3</sub>O. If 2.77 g of the gas occupies 1.00 L at exactly 0°C at a pressure of 760 Torr, what is the molecular formula of the gas?



$$PV = nRT \Rightarrow (1 \text{ atm})(1 \text{ L}) = n(.08206 \text{ L*atm/mol*K})(273K); \quad n = .0446 \text{ moles}$$

$$2.77g / \# \text{ of moles} = 62.1 \text{ g/mol};$$

$$\text{EF mass} = 12.01 + 3(1.01) + 16 = 31.03 \text{ g/mol}$$

$$\text{Multiply by 2 to get } 62.1 \text{ g/mol}$$

$$\text{Therefore, the answer is 2. C}_2\text{H}_6\text{O}_2.$$

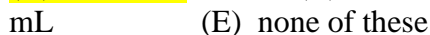
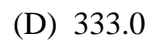
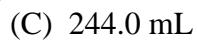
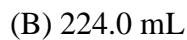
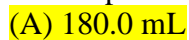
5. In an experiment, 405 mL of methane gas was collected over water with a total pressure of 785 torr at 30°C. What is the vapor pressure of water (in torr) at 30°C if 0.258 g of methane was collected?

$$P_{\text{Total}} = P_{\text{CH}_4} + P_{\text{H}_2\text{O}}$$

$$P_{\text{CH}_4} = \frac{nRT}{V} = \frac{(0.258 \text{ g} \frac{1 \text{ mol}}{16.026 \text{ g}})(0.08206 \frac{\text{atmL}}{\text{molK}})(30+273K)}{0.405L} = 0.988 \text{ atm} \frac{760 \text{ torr}}{1 \text{ atm}} = 751 \text{ torr}$$

$$P_{\text{H}_2\text{O}} = 785 \text{ torr} - 751 \text{ torr} = 34 \text{ torr}$$

6. A 275.0-mL sample of O<sub>2</sub> is collected over water at 60.0°C. The total pressure is 755 torr. What is the volume of the O<sub>2</sub> at STP? (The vapor pressure of water at 60°C is 149 torr).



$$P_{\text{Total}} = P_{\text{O}_2} + P_{\text{H}_2\text{O}}, \quad P_{\text{O}_2} = 755 - 149 = 606 \text{ torr}, \quad V_2 = V_1 * \frac{P_1 * T_2}{P_2 * T_1} = \frac{(275.0 \text{ mL})(606 \text{ torr})(273K)}{(760 \text{ torr})(333K)} = 180 \text{ mL}$$

#### Partial Pressure (P<sub>x</sub>):

The pressure of one of the gases in a mixture

#### Dalton's Law of Partial Pressures:

$$P_{\text{tot}} = P_a + P_b \dots$$

#### Mole Fraction:

$$X_a = n_a/n_{\text{tot}}$$

7. Calculate the density of Hydrogen Bromide gas in g/L at 733 mmHg and 40 °C.

$$PV = nRT \Rightarrow PV = \frac{m}{M_u} RT; \quad \rho = \frac{m}{V}; \quad \frac{P * M_u}{RT} = 3.04 \text{ g/L}$$

8. A mixture of gases contains 0.31 moles of CH<sub>4</sub>, 0.25 moles of C<sub>2</sub>H<sub>6</sub>, and 0.29 moles of C<sub>3</sub>H<sub>8</sub> and the total pressure of the system is 1.50 atm. What is the partial pressure of CH<sub>4</sub>?

$$P(\text{CH}_4) = \frac{n(\text{CH}_4)}{n(\text{tot})} P(\text{tot}) = \frac{(0.31 \text{ mol})}{(0.31 \text{ mol} + 0.25 \text{ mol} + 0.29 \text{ mol})} (1.50 \text{ atm}) = 0.55 \text{ atm}$$

9. A mixture of oxygen and helium is 92.3% by mass oxygen. What is the partial pressure of oxygen if atmospheric pressure is 745 Torr?

*If you had a 100 g sample  $\Rightarrow$  92.3 g of O<sub>2</sub> and 7.7 g of He*

$$\frac{92.3 \text{ g O}_2}{31.998 \text{ g/mol}} = 2.88 \text{ mol O}_2 \qquad \frac{7.7 \text{ g of He}}{4.0026 \text{ g/mol}} = 1.92 \text{ mol He}$$

$$P_{\text{O}_2} = X_{\text{O}_2} P_{\text{total}} = \left( \frac{2.88 \text{ mol O}_2}{4.80 \text{ total mol}} \right) 745 \text{ torr} = 447 \text{ torr}$$

10. Given a cylinder of fixed volume filled with 1 mol of argon gas, which of the following is correct? (Assume all gases obey the ideal gas law.)

- (A) If the temperature of the cylinder is changed from 25°C to 50°C, the pressure inside the cylinder will double.  
 (B) If a second mole of argon is added to the cylinder, the ratio  $T/P$  will remain constant.  
 (C) A cylinder of identical volume filled with the same *pressure* of helium must contain more atoms of gas because He has a smaller atomic radius than argon.  
 (D) Two of these are correct. **(E) None of these is correct.**

11. Which of the following relationships is *not* true?

- (A)  $PV = \text{constant}$  when temperature and moles of gas are held constant.  
 (B)  $V/T = \text{constant}$  when pressure and moles of gas are held constant.  
 (C)  $nT = \text{constant}$  when pressure and volume are held constant.  
 (D)  $P/n = \text{constant}$  when volume and temperature are held constant.  
**(E) All of these are true.**

12. Consider a sample of neon gas in a container fitted with a movable piston (assume the piston is massless and frictionless). The temperature of the gas is increased from 20.0°C to 40.0°C. The density of neon

- (A) increases less than 10%. **(B) decreases less than 10%.** (C) increases more than 10%.  
 (D) decreases more than 10%. (E) does not change.

#### IV. Other Equations of State

The ideal gas law does not account for a couple properties of real gases. Real gases have size and feel attraction.

1. Calculate the pressure exerted by 0.5000 mole of N<sub>2</sub> in a 1.000-L container at 25.0°C. Use the van der Waals equation. (Use your constant sheet to find a and b). Compare this to the answer you would get using the ideal gas law.

$$\left[ P + a \left( \frac{n}{V} \right)^2 \right] (V - nb) = nRT$$

$$P = \frac{nRT}{(V - nb)} - a \left( \frac{n}{V} \right)^2$$

$$P = \frac{(0.500 \text{ mol}) \left( 0.08206 \frac{\text{Latm}}{\text{molK}} \right) (298.2)}{(1 \text{ L} - (0.500 \text{ mol})(0.0391 \text{ L/mol}))} - (1.39 \frac{\text{atmL}^2}{\text{mol}^2}) \left( \frac{0.500 \text{ mol}}{1.0 \text{ L}} \right)^2$$

$$= 12.13 \text{ atm}$$

**Ideal Gas Law:  $PV = nRT$**

**Van der Waals Equation State:**

$$(P + a(n/v)^2)(V - nb) = nRT$$

**a = correction for attraction**

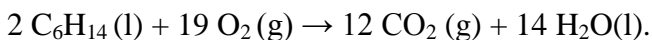
**b = correction for size**

**Virial Equation of State (experimental data)**

$$PV = nRT \left( 1 + B/V_m + C/V_m^2 + \dots \right)$$

## V. Gas Stoichiometry

1. Consider the combustion of liquid hexane



If 1.52-g of hexane is combined with 2.95 L of oxygen at 312K and 890 torr. The carbon dioxide gas is collected at 297 K and 0.930 atm. What volume of carbon dioxide gas will be collected assuming 100% yield?

Need to determine the limiting reagent

$$n_{\text{C}_6\text{H}_{14}} = \frac{1.52 \text{ g}}{86.07 \text{ g/mol}} = 0.0177 \text{ mol vs. } n_{\text{O}_2} = \frac{PV}{RT} = \frac{(890 \text{ torr}/760 \text{ torr/atm})(2.95\text{L})}{(0.08206 \text{ atmL/molK})(312\text{K})} = 0.135 \text{ mol}$$

$$0.135/19 < 0.0177/2 \text{ so } \text{O}_2 \text{ is the LR} \quad 0.135 \text{ mol O}_2 \frac{(12 \text{ mol CO}_2)}{(19 \text{ mol O}_2)} = 0.0853 \text{ mol CO}_2$$

$$V = \frac{nRT}{P} = \frac{(0.0853 \text{ mol})(0.08206 \text{ atmL/molK})(297\text{K})}{(0.93\text{atm})} = 2.23 \text{ L}$$

2. A 3.54-g sample of lead(II) nitrate (molar mass = 331 g/mol) is heated in an evacuated cylinder with a volume of 1.60 L. The salt decomposes when heated, according to the following equation:



Assuming complete decomposition, what is the pressure (in atm) in the cylinder after decomposition and cooling to a temperature of 300. K? Assume the  $\text{PbO}(\text{s})$  takes up negligible volume.

The reaction produces 2 gases so the pressure in the container is the total pressure  $\Rightarrow P_{\text{total}} = \frac{n_{\text{total}}RT}{V}$

$$3.54 \text{ g Pb}(\text{NO}_3)_2 \frac{(1 \text{ mol Pb}(\text{NO}_3)_2)}{(331 \text{ g Pb}(\text{NO}_3)_2)} \times \frac{(4 \text{ mol NO}_2 + 1 \text{ mol O}_2)}{2 \text{ mol Pb}(\text{NO}_3)_2} = 0.0276 \text{ mol gas}$$

$$P_{\text{total}} = \frac{(0.0267 \text{ mol})(0.08206 \text{ atmL/molK})(300\text{K})}{(1.6\text{L})} = 0.41 \text{ atm}$$

3. 2.5 mol of  $\text{O}_2$  gas and 3.0 mol of solid carbon, C (s) are put into a 3.50-liter container at 23°C. If the carbon and oxygen react completely to form CO (g), what will be the final pressure (in atm) in the container at 23°C?



Determine limiting reagent

$$\text{C} \Rightarrow 3 \text{ mol C}/2 = 1.5$$

$$\text{O}_2 \Rightarrow 2.5 \text{ mol}/1 = 2.5 \Rightarrow \text{C is the LR}$$

Since C is the LR  $\Rightarrow$  in addition to the CO formed there will be excess  $\text{O}_2$  in the container so the pressure will be the total pressure

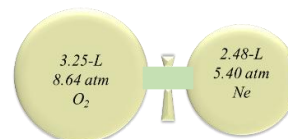
$$\Rightarrow P_{\text{total}} = n_{\text{total}}RT/V$$

$$\text{Since there is 4 mol of gas in the container} \quad P_{\text{total}} = \frac{(4 \text{ mol})(0.08206 \text{ atmL/molK})(23+273 \text{ K})}{3.5 \text{ L}}$$

$$P_{\text{total}} = 27.8 \text{ atm}$$

$2 \text{ C}(\text{s})$	$\text{O}_2(\text{g})$	$\rightarrow$	$2 \text{ CO}(\text{g})$
3 mole	2.5 mole		0 mole
-3	$-3(\frac{1}{2})$		$+3(\frac{2}{2})$
0	1 mole		3 mole

4. The valve between two tanks is opened. See below. Calculate the total pressure in the container after the valve is opened.



Each gas is affected by the valve opening  $\Rightarrow \frac{P_1V_1}{n_1T_1} = \frac{P_2V_2}{n_2T_2}$  where  $n$  and  $T$  are constant

$$\text{solving for } P_2 \Rightarrow P_2 = \frac{P_1V_1}{V_2}$$

$$\text{for O}_2 \Rightarrow P_2 = \frac{(8.64 \text{ atm})(3.25 \text{ L})}{(3.25\text{L}+2.48\text{L})}$$

$$P_2 = 4.9 \text{ atm}$$

$$\text{for Ne} \Rightarrow P_2 = \frac{(5.4 \text{ atm})(2.48 \text{ L})}{(3.25\text{L}+2.48\text{L})} = 2.3 \text{ atm}$$

$$\text{Total pressure} = 4.9 \text{ atm} + 2.3 \text{ atm} = 7.2 \text{ atm}$$