

Lesson 3.5 - Graphs of Logarithmic Equations

I. Warm-Up

1. Rewrite in exponential form. Solve for x. $0 = \log_3(x - 2)$

$$3^0 = x - 2 \quad 1 = x - 2 \quad x = 3$$

$$2. \text{ Evaluate } \log_9(\sqrt{3}) \quad 9^x = \sqrt{3} \quad x = \frac{1}{4}$$

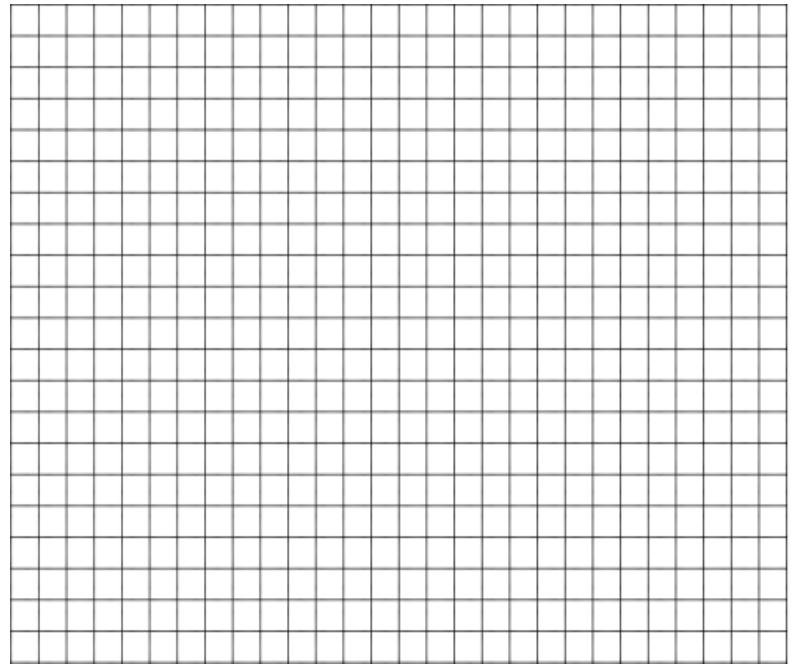
3. Graph (on the same axes & label)

- a. $y = 2^x$
- b. $y = 2^{-x}$
- c. $y = \left(\frac{1}{2}\right)^x$
- d. Inverse of part a.

Check on Desmos.

Properties of Log Graphs

Domain – make the inside > 0 .
A vertical asymptote will mark the restricted domain.

**II. Practice** – For each of the functions find:

- (a) The domain. (b). the vertical asymptotes (c). the intercepts

4. $f(x) = \log_6(x - 1)$

Vertical Asymptote: $x = 1$

Domain: $\{x|x > 1\}$

x-intercept: $(2, 0)$

y-intercept: none

5. $g(x) = \log_2(x + 1) - 3$

Vertical Asymptote: $x = -1$

Domain: $\{x|x > -1\}$

x-intercept: $(7, 0)$

y-intercept: $(0, -3)$

6. $h(x) = \log_3(-x + 3) + 2$

Vertical Asymptote: $x = 3$

Domain: $\{x|x < 3\}$

x-intercept: $(2\frac{8}{9}, 0)$

y-intercept: $(0, 3)$

Find the domain, vertical asymptotes, and intercepts for each function. Then sketch a graph.

7. $f(x) = \log_3(1 - x)$

Vertical Asymptote: $x = 1$

Domain: $\{x | x < 1\}$

$$0 = \log_3(1 - x)$$

$$3^0 = 1 - x$$

$$x = 0$$

x-intercept: $(0, 0)$

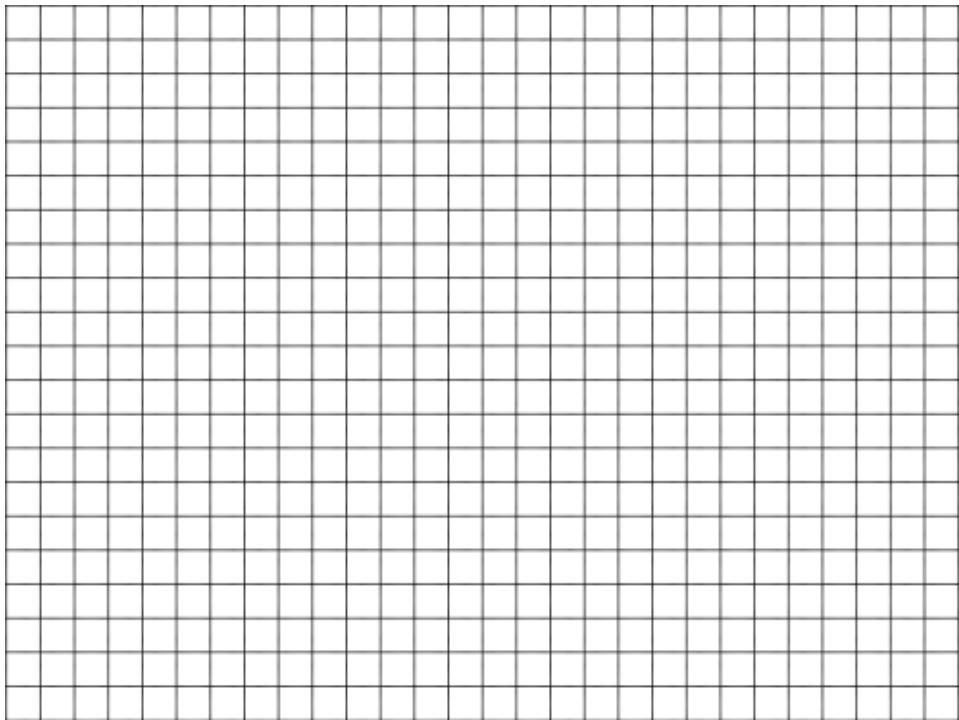
$$f(x) = \log_3(1 - 0)$$

$$f(x) = \log_3(1)$$

$$f(x) = 0$$

y-intercept: $(0, 0)$

Check graph on Desmos.



8. $f(x) = \log_4(x - 3) + 1$

Vertical Asymptote: $x = 3$

Domain: $\{x | x > 3\}$

$$0 = \log_4(x - 3) + 1$$

$$-1 = \log_4(x - 3)$$

$$4^{-1} = x - 3$$

$$x = \frac{1}{4} + 3 = 3\frac{1}{4}$$

x-intercept: $(3.25, 0)$

$$f(x) = \log_4(0 - 3) + 1$$

$$f(x) = \log_3(-3) + 1$$

y-intercept: none

Check graph on Desmos.



$$9. \ f(x) = -\ln(x + 2)$$

Vertical Asymptote: $x = -2$

Domain: $\{x|x > -2\}$

$$0 = -\ln(x + 2)$$

$$e^0 = x + 2 = 1$$

$$x = -1$$

x-intercept: $(-1, 0)$

$$f(x) = \ln(0 + 2)$$

$$f(x) = -\ln(2)$$

y-intercept: $(0, -\ln(2))$

Check graph on Desmos.



$$10. \ f(x) = \ln(4 - x)$$

Vertical Asymptote: $x = 4$

Domain: $\{x|x > 4\}$

$$0 = \ln(4 - x)$$

$$e^0 = 4 - x$$

$$x = 3$$

x-intercept: $(3, 0)$

$$f(x) = \ln(4 - 0)$$

$$f(x) = \ln(4)$$

y-intercept: $(0, \ln(4))$

Check graph on Desmos.

