Lesson 1.3 – Solving Linear & Rational Linear Equations (pages 81-90, 154-156 in Red 9/10 textbook)

## I. **Warm-up: Balancing Equations**

For any equation the left-hand side must always equal the right-hand side. If we add/subtract/multiply/divide the same number of both sides, the equation is still true.

- 1. Write down the equation that results when:
  - a. 5 is added to both sides of 2x 5 = 7

$$2x = 12$$

b. 3 is taken from both sides of 5x + 3 = 18

$$5x = 15$$

c. Both sides of  $\frac{3x-2}{4} = -1$  are multiplied by 4.

$$3x - 2 = -4$$

d. Both sides of 5x = -15 are divided by 5.

$$x = -3$$

## II. **Linear Equations: Solving for x**

2. Solve for x: 3x + 7 = 22.

Plug your solution back in for x to check.

$$3x = 15$$
  $x = 5$ 

3. Solve for x: 11 - 5x = 26. Plug your solution back in for x to check.

$$-5x = 15$$
  $x = -3$ 

4. Solve for x:  $\frac{x}{3} + 2 = -2$ . Plug your solution back in for x to check.

$$\frac{x}{3} = -4$$
  $x = -12$ 

5. Solve for x:  $\frac{4x+3}{5} = -2$ . Plug your solution back in for x to check.

$$4x + 3 = -10 \qquad 4x = -13 \qquad x = -\frac{13}{4}$$

6. Solve for x: 5(x+1) - 2x = -7. Plug your solution back in for x to check.

$$5x + 5 - 2x = -7$$
  $3x = -12$   $x = -4$ 

7. Solve for x: 5x + 2 = 3x - 5. Plug your solution back in for x to check.

$$5x + 2 = 3x - 5$$
  $2x = -7$   $x = -\frac{7}{2}$ 

8. Solve for x:  $\frac{2x+3}{4} = \frac{x-2}{3}$ . Plug your solution back in for x to check.

$$3(2x+3) = 4(x-2)$$
  $6x + 9 = 4x - 8$   $2x = -17$   $x = -\frac{17}{2}$ 

## III. Practice on Your Own

9. Solve the equation 
$$-8 + 9r = -5r$$

$$-8 = -14r \qquad \qquad r = 4/7$$

10. Solve the equation 
$$6x + 5 = 4$$

$$6x = -1$$
  $x = -1/6$ 

11. Solve the equation 
$$10(x+4) = 5x + 5$$

$$10x + 40 = 5x + 5$$
  $5x = -35$   $x = -7$ 

12. Solve the equation 
$$6(b+1) + 5 = -6(b-4) - 7$$

$$6b + 6 + 5 = -6b + 24 - 7$$
  $6b + 11 = -6b + 17$   $12b = 6$   $b = 1/2$ 

13. Solve the equation 
$$\frac{7b+4}{2b-6} = \frac{7}{10}$$

$$10(7b+4) = 7(2b-6)$$
  $70b+40 = 14b-42$   $56b = -82$   $b = -41/28$ 

14. Solve the equation 
$$\frac{5}{5-a} = \frac{7}{a-2}$$

$$5(a-2) = 7(5-a)$$
  $5a-10 = 35-7a$   $12a = 45$   $a = 15/4$ 

15. Solve the equation 
$$\frac{2}{x} = \frac{3}{4x} + 5$$

$$\frac{8}{4x} = \frac{3}{4x} + \frac{5(4x)}{4x} \qquad 8 = 3 + 20x \qquad 5 = 20x \qquad x = 1/4$$

16. Solve the equation 
$$\frac{x}{7x-3} = \frac{3}{5}$$

$$5x = 3(7x - 3)$$
  $5x = 21x - 9$   $-16x = -9$   $x = 9/16$ 

17. Solve the equation 
$$4x - \frac{1}{2}(5 - x) = -\frac{1}{4}(x + 6)$$

$$4x - \frac{5}{2} + \frac{1}{2}x = -\frac{1}{4}x - \frac{3}{2} \qquad 4x + \frac{1}{2}x + \frac{1}{4}x = \frac{5}{2} - \frac{3}{2} \qquad \frac{16}{4}x + \frac{2}{4}x + \frac{1}{4}x = 1 \qquad \frac{19}{4}x = 1$$

$$x = 4/19$$

18. Solve the equation 
$$0.4(g-9) = 0.9(g-2)$$

$$0.4g - 3.6 = 0.9g - 1.8$$
  $-1.8 = 0.5g$   $g = -3.6$ 

19. Solve the equation 
$$-\frac{1}{3}k + \left(-\frac{2}{5}\right) = 1 - \left(-\frac{5}{6}k\right)$$
  
 $-\frac{1}{3}k - \frac{2}{5} = 1 + \frac{5}{6}k$   $-\frac{2}{6}k - \frac{5}{6}k = 1 + \frac{2}{5}$   $\frac{-7}{6}k = \frac{7}{5}$   $k = -\frac{6}{5}$ 

20. Solve the equation 
$$7(x + 3) = 4(x + 3) + 2$$

$$7x + 21 = 4x + 12 + 2$$
  $7x + 21 = 4x + 14$   $3x = -7$   $x = -7/3$ 

21. Solve the equation 
$$9(x - 38778869) + 2 = -3(x - 38778869) - 22$$

$$9x - 9(38778869) + 2 = -3x + 3(38778869) - 22$$

$$12x = 12(38778869) - 24$$

$$x = 38778869 - 2 = 38778867$$

## IV. Rational Equations

For rational equations, write all fractions with the same lowest common denominator, then equate the numerators.

22. Solve for x: 
$$\frac{6}{x} = \frac{2}{3}$$
. Plug your solution back in for x to check.

$$18 = 2x$$
  $x = 9$ 

23. Solve for x: 
$$\frac{5}{x+2} = \frac{2}{x-1}$$
. Plug your solution back in for x to check.

$$5(x-1) = 2(x+2)$$
  $5x-5 = 2x+4$   $3x = 9$   $x = 3$ 

24. Solve for x: 
$$\frac{-4x}{x-8} - \frac{11}{x-8} = \frac{25}{x-8}$$
.

$$-4x - 11 = 25$$
  $-4x = 36$   $x = -6$ 

25. Solve for x: 
$$\frac{3}{4} - \frac{2x}{4x - 24} = \frac{8}{x - 6}$$
.

$$\frac{3(x-6)}{4(x-6)} - \frac{2x}{4x-24} = \frac{4(8)}{4(x-6)} \qquad 3x - 18 - 2x = 32 \qquad x = 50$$

26. Solve for x: 
$$\frac{3}{6x} - \frac{9}{12} = \frac{11}{4x}$$
.

$$\frac{2(3)}{2(6x)} - \frac{9x}{12x} = \frac{3(11)}{3(4x)}. \qquad 6 - 9x = 33 \qquad -9x = 27 \qquad x = -3$$

27. Solve for x: 
$$\frac{18}{5x-10} + \frac{4}{5} = \frac{-6}{x-2}$$
.

$$\frac{18}{5x-10} + \frac{4(x-2)}{5(x-2)} = \frac{5(-6)}{5(x-2)}$$

$$18 + 4(x-2) = -30$$

$$18 + 4x - 8 = -30.$$

$$4x = -40$$

$$x = -10$$

28. Solve for x: 
$$\frac{12}{x^2+5x+6} + \frac{7}{x+3} = \frac{2}{x+2}$$

$$x = -4$$

29. Solve for x: 
$$\frac{1}{10} + \frac{4x}{5x} = \frac{-9}{2x}$$
.

$$\frac{1(x)}{10(x)} + \frac{2(4x)}{2(5x)} = \frac{5(-9)}{5(2x)}.$$
  $x + 8x = -45$   $9x = -45$   $x = -5$ 

30. Solve for x: 
$$\frac{2}{x-6} + \frac{7}{x+2} = \frac{4x+2}{x^2-4x-12}$$
.

$$\frac{2(x+2)}{(x-6)(x+2)} + \frac{7(x-6)}{(x+2)(x-6)} = \frac{4x+2}{x^2-4x-12} \qquad 2x+4+7x-42 = 4x+2 \qquad 9x-38 = 4x+2$$

$$5x = 40 \qquad x = 8$$